

TRIAL NEGERI
2022
VECTOR ADD
MATHS SPM

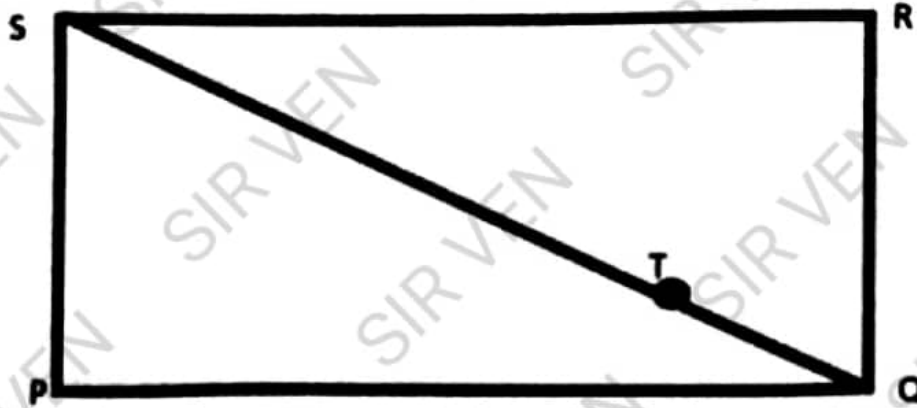


SIR VEN

Q1: PERLIS

Rajah 3 menunjukkan sebuah segiempat tepat PQRS. T ialah titik yang terletak pada QS dengan keadaan $QS = 4QT$.

Diagram 3 shows a rectangle PQRS. T is a point which lies on QS such that $QS = 4QT$.



Rajah 3/ Diagram 3

- (a) Diberi $\overrightarrow{QP} = 15x$ dan $\overrightarrow{QS} = 15x + 7y$, ungkapkan vector yang berikut dalam sebutan x dan y .

Given that $\overrightarrow{QP} = 15x$ and $\overrightarrow{QS} = 15x + 7y$, express the following vectors in terms of x and y

- (i) $\overrightarrow{QT}$
- (ii) $\overrightarrow{PT}$

- (b) Diberi garis lurus PT dipanjangkan ke titik U dengan keadaan $\overrightarrow{PU} = -9x + ky$.

Cari nilai k .

Given that straight line PT is extended to the point U such that $\overrightarrow{PU} = -9x + ky$.

Find the value k .

[7 markah/7 marks]

Jawapan/ Answer :

3

(a)

Tulis hukum segitiga

K1

$$\overrightarrow{PT} = \overrightarrow{PQ} + \overrightarrow{QT}$$

$$\frac{15}{4}x + \frac{7}{4}y \quad \boxed{\text{N1}} \quad \boxed{\text{N1}} \quad \frac{-45}{4}x + \frac{7}{4}y$$

(b)

Guna $\overrightarrow{PU} = \lambda \overrightarrow{PT}$

P1

Samakan pekali x dan y

K1

$$\frac{45}{4}\lambda = 9 \quad \text{atau} \quad \frac{7}{4}\lambda = k$$

N1

$$\lambda = \frac{4}{5}$$

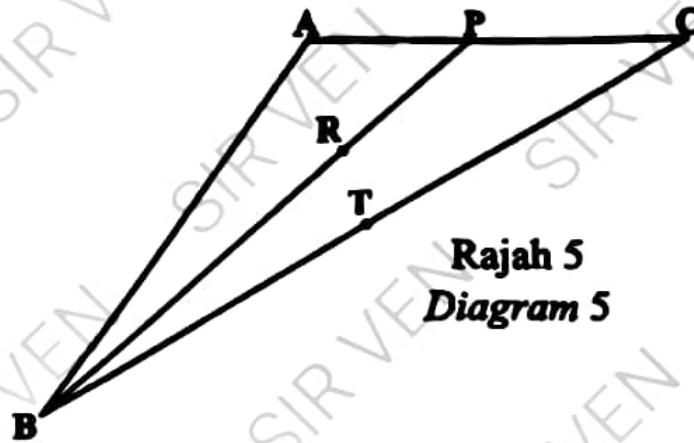
N1

$$k = \frac{7}{5}$$

Q2: YIK KELANTAN

Rajah 5 menunjukkan sebuah segi tiga ABC . Titik R terletak pada BP dan titik T terletak pada BC .

Diagram 5 shows a triangle ABC . Point R lies on BP and point T lies on BC .



Diberi bahawa, $\overline{AB} = 6x$, $\overline{AC} = 4y$, $3AP = PC$ dan titik T adalah titik tengah bagi BC .

It is given that $\overline{AB} = 6x$, $\overline{AC} = 4y$, $3AP = PC$ and point T is the midpoints of BC .

(a) Ungkapkan dalam sebutan x dan y

Express in terms of x and y

(i) $\overline{BC}$,

(ii) $\overline{AT}$.

[4 markah]

[4 marks]

(b) Diberi bahawa $\overline{AR} = m\overline{AT}$ dan $\overline{AR} = \overline{AP} - n\overline{BP}$, dengan keadaan m dan n ialah pemalar.

It is given that $\overline{AR} = m\overline{AT}$ and $\overline{AR} = \overline{AP} - n\overline{BP}$, where m and n are constants.

Cari nilai m dan nilai n .

Find the values of m and of n .

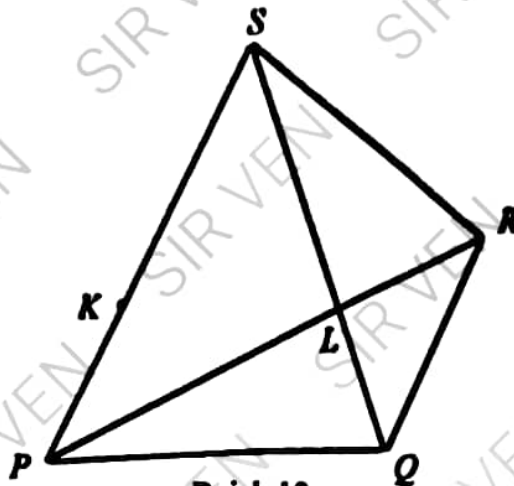
[6 markah]

[6 marks]

Q3: SAMK (ASRAMA)

Rajah 10 menunjukkan sebuah sisi empat PQRS.

Diagram 10 shows a quadrilateral PQRS.



Rajah 10
Diagram 10

Diberi bahawa $\overline{PK} = 2x$, $\overline{PQ} = 3y$, $PK : PS = 1 : 3$ dan $2QL = LS$.

It is given that $\overline{PK} = 2x$, $\overline{PQ} = 3y$, $PK : PS = 1 : 3$ and $2QL = LS$.

(a) Ungkapkan dalam sebutan x dan/ atau y :

Express in terms of x and / or y :

(i) $\overline{SQ}$

(ii) $\overline{PL}$

[3 markah]

[3 marks]

(b) Diberi bahawa $\overline{SR} = 2ay - 2x$ dan $\overline{PR} = \frac{1}{b} \overline{PL}$, dengan keadaan a dan b ialah pemalar.

Given that $\overline{SR} = 2ay - 2x$ and $\overline{PR} = \frac{1}{b} \overline{PL}$, such that a and b are constants.

Cari

Find

(i) $\overline{SR}$ dalam sebutan b , x dan y ,

$\overline{SR}$ in terms of b , x and y ,

(ii) nilai a dan b .

the value of a and of b .

[5 markah]

[5 marks]

(c) Diberi luas segi tiga PQS adalah 120 unit², dan jarak serenjang dari Q ke PS ialah 5 unit, cari $|x|$.

Given the area of PQS is 120 unit², and the perpendicular distance from Q to PS is 5 unit, find $|x|$.

[2 markah]

[2 marks]

(a)(i)

$$\overline{SQ} = -6\bar{x} + 3\bar{y}$$

(ii)

$$\overline{PL} = 3\bar{y} + \frac{1}{3}(6\bar{x} - 3\bar{y})$$

$$\overline{PL} = 2\bar{x} + 2\bar{y}$$

10

$$\overline{PR} = \frac{1}{b}(2\bar{x} + 2\bar{y})$$

(b)(i)

$$\overline{PR} = \frac{2}{b}\bar{x} + \frac{2}{b}\bar{y}$$

$$\overline{SR} = \overline{SP} + \overline{PR}$$

$$\overline{SR} = \left(-6 + \frac{2}{b}\right)\bar{x} + \frac{2}{b}\bar{y}$$

(b)(ii)

Perbandingan & menyelesaikan persamaan serentak

Comparison & solving using simultaneous equation

$$-6 + \frac{2}{b} = -2 \quad \text{or} \quad 2a = \frac{2}{b}$$

$$a = 2$$

$$b = \frac{1}{2}$$

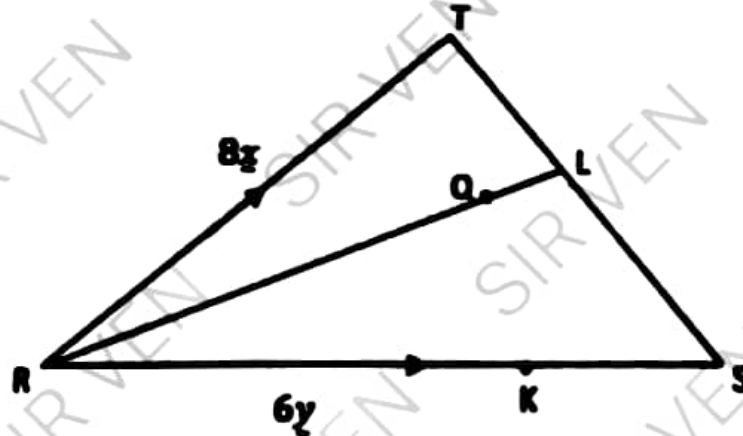
(c)

$$\frac{1}{2}(6|\bar{x}|)(5) = 120$$

$$|\bar{x}| = 8 \text{ unit}$$

Q4: MELAKA

Rajah 2 menunjukkan sebuah segi tiga RST
Diagram 2 shows a triangle RST



Rajah 2 / Diagram 2

Titik L terletak di atas garis lurus TS dengan keadaan $TS = 3TL$. Diberi bahawa $\overrightarrow{RT} = 8x$, $\overrightarrow{RK} = 6y$, $\overrightarrow{KS} = 4y$ dan $\overrightarrow{RQ} = n\overrightarrow{RL}$

Point L lies on the straight line TS such that $TS = 3TL$. It is given that $\overrightarrow{RT} = 8x$, $\overrightarrow{RK} = 6y$, $\overrightarrow{KS} = 4y$ and $\overrightarrow{RQ} = n\overrightarrow{RL}$

(a) Ungkapkan dalam sebutan x dan y bagi
Express in terms of x and y of

(i) $\overrightarrow{TS}$

[3 markah]

(ii) $\overrightarrow{TK}$

[3 marks]

(b) (i) Ungkapkan $\overrightarrow{TQ}$ dalam sebutan n , x dan y .

[2 markah]

Express $\overrightarrow{TQ}$ in terms of n , x and y .

[2 marks]

(ii) Seterusnya, cari nilai bagi n jika titik - titik T, Q dan K adalah segaris. [3 markah]

Hence, find the value of n if point T, Q and K are collinear.

[3 marks]

(a) i. $\overrightarrow{TS} = \overrightarrow{TR} + \overrightarrow{RS}$ or $\overrightarrow{TK} = \overrightarrow{TR} + \overrightarrow{RK}$

$$\overrightarrow{TS} = -8\hat{x} + 10\hat{y}$$

ii. $\overrightarrow{TK} = -8\hat{x} + 6\hat{y}$

(b) i. $\overrightarrow{TQ} = \overrightarrow{TR} + \overrightarrow{RQ}$

$$= -8\hat{x} + n(\overrightarrow{RL})$$

$$= -8\hat{x} + n(\overrightarrow{RT} + \overrightarrow{TL})$$

$$= -8\hat{x} + n(8\hat{x} + \frac{1}{3}(-8\hat{x} + 10\hat{y}))$$

$$= -8\hat{x} + \frac{16}{3}n\hat{x} + \frac{10}{3}n\hat{y}$$

$$\overrightarrow{TQ} = \left[\frac{16}{3}n - 8 \right] \hat{x} + \frac{10}{3}n\hat{y}$$

ii.

$$\left[\frac{16n}{3} - 8 \right] \hat{x} + \frac{10}{3}n\hat{y} = \lambda[-8\hat{x} + 6\hat{y}] \quad \text{or equivalent}$$

$$-8\lambda = \frac{16n}{3} - 8 \quad \text{or} \quad \frac{10n}{3} = 6\lambda$$

$$n = \frac{9}{11}$$

Q5: KELANTAN MMIS SET 1

Rajah 4 menunjukkan segi tiga OAR dan segi tiga OPB . Titik P dan R masing-masing terletak pada garis lurus OA dan garis lurus OB . Garis lurus AR dan garis lurus BP bersilang pada titik Q .

Diagram 4 shows triangle OAR and triangle OPB . The point P and R lies on straight line OA and straight line OB respectively. The straight line AR intersects the straight line BP at the point Q .



Rajah 4

Diagram 4

Diberi bahawa $\overrightarrow{OA} = 12\mathbf{u}$, $\overrightarrow{OB} = 10\mathbf{v}$, $\overrightarrow{OQ} = 4\overrightarrow{PA}$ dan $\overrightarrow{OR} = 2\overrightarrow{RB}$.

It is given that $\overrightarrow{OA} = 12\mathbf{u}$, $\overrightarrow{OB} = 10\mathbf{v}$, $\overrightarrow{OQ} = 4\overrightarrow{PA}$ and $\overrightarrow{OR} = 2\overrightarrow{RB}$.

(a) Ungkapkan dalam sebutan $\mathbf{u}$ dan $\mathbf{v}$:

Express in terms of $\mathbf{u}$ and $\mathbf{v}$:

(i) $\overrightarrow{BP}$

(ii) $\overrightarrow{AR}$

[3 markah]

[3 marks]

(b) Diberi bahawa $\overrightarrow{OQ} = m\overrightarrow{AR}$, dan $\overrightarrow{BQ} = n\overrightarrow{BP}$, dengan keadaan m dan n ialah pemalar. Ungkapkan $\overrightarrow{OQ}$ dalam sebutan

It is given that $\overrightarrow{OQ} = m\overrightarrow{AR}$ and $\overrightarrow{BQ} = n\overrightarrow{BP}$, where m and n are constants.

Express $\overrightarrow{OQ}$ in terms of

(i) m , $\mathbf{u}$ dan $\mathbf{v}$.

m , $\mathbf{u}$ and $\mathbf{v}$.

(ii) n , $\mathbf{u}$ dan $\mathbf{v}$.

n , $\mathbf{u}$ and $\mathbf{v}$.

Seterusnya, cari nilai m dan nilai n .

[5 markah]

Hence, find the value of m and of n .

[5 marks]

(c) Diberi $|\mathbf{u}| = 3$ unit, $|\mathbf{v}| = 2$ unit dan $\angle AOB = 90^\circ$, cari $|\overrightarrow{AB}|$.

[2 markah]

Given that $|\mathbf{u}| = 3$ unit, $|\mathbf{v}| = 2$ unit and $\angle AOB = 90^\circ$, find $|\overrightarrow{AB}|$.

[2 marks]

$$b)(a) \quad \overrightarrow{BP} = \overrightarrow{BO} + \overrightarrow{OP} \quad \text{or} \quad \overrightarrow{AR} = \overrightarrow{AO} + \overrightarrow{OR}$$

$$\overrightarrow{BP} = -10\hat{v} + 9\hat{u}$$

$$\overrightarrow{AR} = -12\hat{u} + \frac{20}{3}\hat{v}$$

$$b)(i) \quad \overrightarrow{OQ} = m \left(-12\hat{u} + \frac{20}{3}\hat{v} \right)$$

$$(ii) \quad \overrightarrow{OQ} = 9n\hat{u} + (10 - 10n)\hat{v}$$

$$-12m\hat{u} + \frac{20}{3}m\hat{v} = 9n\hat{u} + (10 - 10n)\hat{v}$$

$$-12m = 9n \quad \text{or} \quad \frac{20}{3}m = 10 - 10n$$

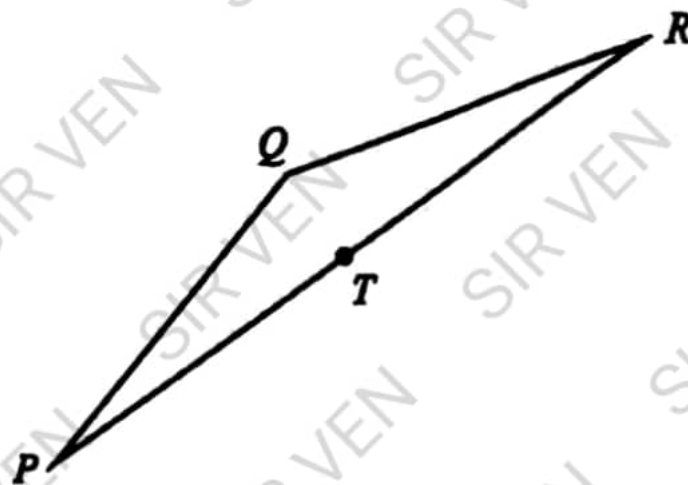
$$m = -\frac{3}{2}, \quad n = 2$$

$$(c) \quad |\overrightarrow{AB}| = \sqrt{(-12(3))^2 + (10(2))^2}$$

$$= 41.18 // 4\sqrt{106}$$

Q6: SELANGOR (SET 2)

Rajah 1 menunjukkan sebuah segi tiga PQR . T ialah titik tengah garis lurus PR .
Diagram 1 shows a triangle PQR . T is the midpoint of the straight line PR .



Rajah 1
Diagram 1

Diberi bahawa koordinat P ialah $(2, -1)$, $\vec{PQ} = \begin{pmatrix} 4 \\ 3 \end{pmatrix}$ dan $\vec{TR} = \begin{pmatrix} 5 \\ 2 \end{pmatrix}$.

It is given that coordinates P is $(2, -1)$, $\vec{PQ} = \begin{pmatrix} 4 \\ 3 \end{pmatrix}$ and $\vec{TR} = \begin{pmatrix} 5 \\ 2 \end{pmatrix}$.

(a) Tunjukkan koordinat bagi titik:

Show that the coordinates of the point:

(i) Q ialah $(6, 2)$.

Q is $(6, 2)$.

(ii) R ialah $(12, 3)$.

R is $(12, 3)$.

[4 markah]

[4 marks]

(b) Tentukan vektor unit dalam arah vektor $\vec{QT}$.

Berikan jawapan anda dalam bentuk surd yang teringkas.

Determine the unit vector in the direction of vector $\vec{QT}$.

Give your answer in the simplest surd form.

[4 markah]

[4 marks]

$$(a) (i) \overrightarrow{OQ} = \overrightarrow{OP} + \overrightarrow{PQ} \text{ atau } \overrightarrow{OP} = 2\mathbf{i} - \mathbf{j} \text{ atau } \overrightarrow{OP} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$= (2\mathbf{i} - \mathbf{j}) + (4\mathbf{i} + 3\mathbf{j}) \text{ atau } \begin{pmatrix} 2 \\ -1 \end{pmatrix} + \begin{pmatrix} 4 \\ 3 \end{pmatrix}$$

$$(6, 2)$$

$$(ii) \overrightarrow{OR} = \overrightarrow{OP} + 2\overrightarrow{PR}$$

$$= (2\mathbf{i} - \mathbf{j}) + 2(5\mathbf{i} + 2\mathbf{j}) \text{ atau } \begin{pmatrix} 2 \\ -1 \end{pmatrix} + 2\begin{pmatrix} 5 \\ 2 \end{pmatrix}$$

$$(12, 3)$$

$$(b) \overrightarrow{QT} = (6\mathbf{i} + \mathbf{j}) + (-5\mathbf{i} - 2\mathbf{j}) \text{ atau } \begin{pmatrix} 6 \\ 1 \end{pmatrix} + \begin{pmatrix} -5 \\ -2 \end{pmatrix} \text{ ATAU } \begin{pmatrix} -4 \\ -3 \end{pmatrix} + \begin{pmatrix} 5 \\ 2 \end{pmatrix}$$

$$= \mathbf{i} - \mathbf{j} \quad \text{atau} \quad = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$|\overrightarrow{QT}| = \sqrt{(1)^2 + (-1)^2}$$

$$= \sqrt{2}$$

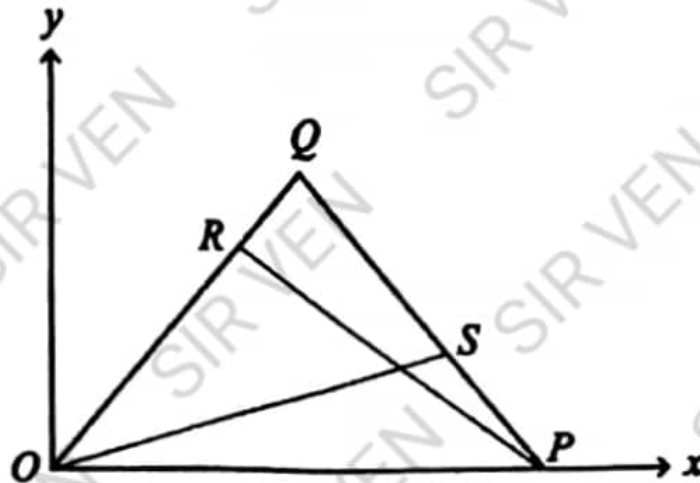
$$\frac{1}{\sqrt{2}}(\mathbf{i} - \mathbf{j}) \text{ ATAU } \frac{1}{\sqrt{2}}\begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$\frac{\sqrt{2}}{2}\mathbf{i} - \frac{\sqrt{2}}{2}\mathbf{j} \text{ ATAU } \begin{pmatrix} \frac{\sqrt{2}}{2} \\ -\frac{\sqrt{2}}{2} \end{pmatrix}$$

Q7: SELANGOR (SET 1)

Rajah 1 menunjukkan sebuah segi tiga OPQ di satah Cartes dan O ialah asalan. Diberi R dan S masing-masing berada atas garis lurus OQ dan PQ di mana $OR : RQ = 2 : 1$ dan $QS = 5SP$.

Diagram 1 shows a triangle OPQ on a Cartesian plane and O is the origin. Given that R and S lie on the straight line OQ and PQ respectively where $OR : RQ = 2 : 1$ and $QS = 5SP$.



Rajah 1
Diagram 1

Diberi bahawa $\vec{OP} = 6\mathbf{i}$ dan $\vec{OR} = 2\mathbf{i} + 4\mathbf{j}$.

It is given that $\vec{OP} = 6\mathbf{i}$ and $\vec{OR} = 2\mathbf{i} + 4\mathbf{j}$.

(a) Cari koordinat bagi titik:

Find the coordinates of the point:

(i) Q ,

(ii) S .

[4 markah]

[4 marks]

(b) Tentukan vektor unit dalam arah vektor $\vec{RS}$.

Berikan jawapan anda dalam bentuk surd yang teringkas.

Determine the unit vector in the direction of vector $\vec{RS}$.

Give your answer in the simplest surd form.

[4 markah]

[4 marks]

$$(a) (i) \frac{3}{2}(2\mathbf{i} + 4\mathbf{j}) \text{ ATAU } \frac{3}{2} \begin{pmatrix} 2 \\ 4 \end{pmatrix}$$

$$3\mathbf{i} + 6\mathbf{j} \text{ ATAU } \begin{pmatrix} 3 \\ 6 \end{pmatrix}$$

$$(3, 6)$$

$$(ii) \overrightarrow{OS} = \overrightarrow{OP} + \frac{1}{6}\overrightarrow{PQ} \text{ ATAU } \overrightarrow{OS} = \overrightarrow{OQ} + \frac{5}{6}\overrightarrow{QP}$$

$$6\mathbf{i} + \frac{1}{6}(-6\mathbf{i} + (3\mathbf{i} + 6\mathbf{j})) \text{ ATAU } \begin{pmatrix} 6 \\ 0 \end{pmatrix} + \frac{1}{6} \begin{pmatrix} -6 + 3 \\ 6 \end{pmatrix}$$

$$(3\mathbf{i} + 6\mathbf{j}) + \frac{5}{6}(-3\mathbf{i} - 6\mathbf{j} + 6\mathbf{i}) \text{ ATAU } \begin{pmatrix} 3 \\ 6 \end{pmatrix} + \frac{5}{6} \begin{pmatrix} -3 + 6 \\ -6 \end{pmatrix}$$

$$\left(\frac{11}{2}, 1\right)$$

$$(b) -2\mathbf{i} - 4\mathbf{j} + \frac{11}{2}\mathbf{i} + \mathbf{j} \text{ ATAU } \begin{pmatrix} -2 \\ -4 \end{pmatrix} + \begin{pmatrix} \frac{11}{2} \\ 1 \end{pmatrix}$$

$$\frac{7}{2}\mathbf{i} - 3\mathbf{j} \text{ ATAU } \begin{pmatrix} \frac{7}{2} \\ -3 \end{pmatrix}$$

$$\sqrt{\left(\frac{7}{2}\right)^2 + (-3)^2}$$

$$\frac{\sqrt{85}}{2}$$

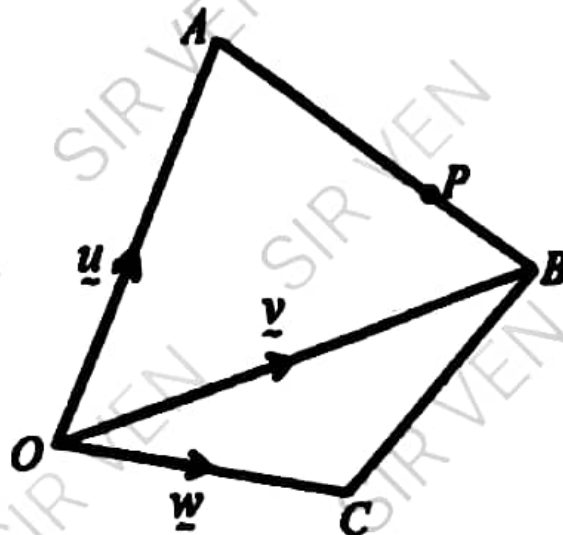
$$\frac{1}{\frac{\sqrt{85}}{2}} \left(\frac{7}{2}\mathbf{i} - 3\mathbf{j} \right) \text{ ATAU } \frac{1}{\frac{\sqrt{85}}{2}} \begin{pmatrix} \frac{7}{2} \\ -3 \end{pmatrix}$$

$$\frac{7\sqrt{85}}{85}\mathbf{i} - \frac{6\sqrt{85}}{85}\mathbf{j} \text{ ATAU } \begin{pmatrix} \frac{7\sqrt{85}}{85} \\ -\frac{6\sqrt{85}}{85} \end{pmatrix}$$

Q8: KEDAH

Rajah 7 menunjukkan sisi empat $OABC$ dengan keadaan O ialah asalan. Titik P terletak di atas garis AB dengan keadaan $AP:AB=3:4$ manakala titik Q terletak di atas garis OC dengan keadaan $OQ:OC=2:3$.

Diagram 7 shows that quadrilateral of $OABC$ such as O is origin. The point P lies on AB such that $AP:AB=3:4$ while the point Q lies on the line OC such that $OQ:OC=2:3$.



Rajah 7
Diagram 7

Ungkapkan,
Express,

- (a) (i) $\overrightarrow{AP}$ dalam sebutan $\underline{u}$ dan $\underline{v}$. Seterusnya tunjukkan bahawa $\overrightarrow{OP} = \frac{1}{4}(\underline{u} + 3\underline{v})$.

$\overrightarrow{AP}$ in terms of $\underline{u}$ and $\underline{v}$. Hence show that $\overrightarrow{OP} = \frac{1}{4}(\underline{u} + 3\underline{v})$.

- (ii) $\overrightarrow{PQ}$ dalam sebutan $\underline{u}$, $\underline{v}$ dan $\underline{w}$.

$\overrightarrow{PQ}$ in terms of $\underline{u}$, $\underline{v}$ and $\underline{w}$.

[4 markah / marks]

- (b) Diberi $\overrightarrow{SPQ} = 6\overrightarrow{BC}$, cari $\underline{w}$ dalam sebutan $\underline{u}$ dan $\underline{v}$.

Given that $\overrightarrow{SPQ} = 6\overrightarrow{BC}$, find $\underline{w}$ in terms of $\underline{u}$ and $\underline{v}$.

[3 markah / marks]

(a)(i)

$$\overrightarrow{AP} = \frac{3}{4}(\overrightarrow{AO} + \overrightarrow{OB}) \text{ tulis Hukum K1}$$

$$\overrightarrow{AP} = -\frac{3}{4}\underline{\underline{u}} + \frac{3}{4}\underline{\underline{v}}$$

$$\overrightarrow{OP} = \underline{\underline{u}} + \frac{3}{4}\underline{\underline{v}} - \frac{3}{4}\underline{\underline{u}} \text{ N1}$$

$$\overrightarrow{OP} = \frac{1}{4}(\underline{\underline{u}} + 3\underline{\underline{v}}) \text{ Terbukti N1}$$

(a)(ii)

$$\overrightarrow{PQ} = -\frac{1}{4}\underline{\underline{u}} - \frac{3}{4}\underline{\underline{v}} + \frac{2}{3}\underline{\underline{w}} \text{ N1}$$

(b)

$$\overrightarrow{BC} = \overrightarrow{BA} + \overrightarrow{AO} + \overrightarrow{OC} \text{ Tulis hukum K1}$$

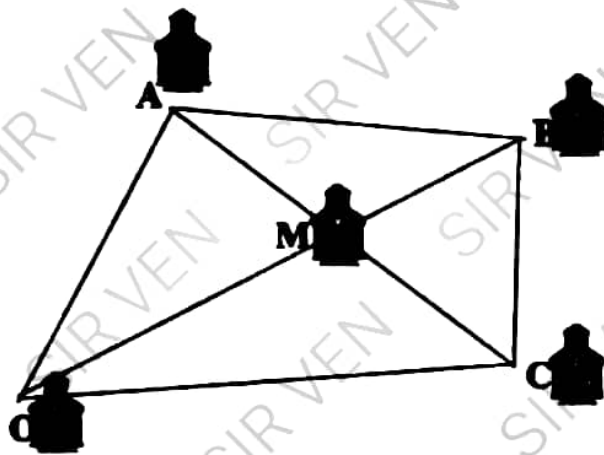
$$-\frac{1}{4}\underline{\underline{u}} - \frac{3}{4}\underline{\underline{v}} + \frac{2}{3}\underline{\underline{w}} = \frac{6}{5}(-\underline{\underline{v}} + \underline{\underline{w}}) \text{ K1}$$

$$\underline{\underline{w}} = \frac{27\underline{\underline{v}} - 15\underline{\underline{u}}}{32} \text{ N1}$$

Q9: PAHANG

Rajah 1 di bawah menunjukkan jalan bagi sekolah-sekolah di sebuah bandar yang berbentuk sisi empat OABC.

The diagram 1 below shows roads of schools in a town area that form a rectangle OABC.



Rajah 1/Diagram 1

Sekolah M terletak di tengah-tengah sekolah A dan C dan $OM : OB = 2 : 3$. Diberi $\vec{OA} = 3\vec{x} + 2\vec{y}$, $\vec{OC} = 9\vec{x} + 2\vec{y}$ dan $\vec{CB} = 3r\vec{y}$, dengan r ialah pemalar,

School M is allocated at the middle of schools A and C and $OM : OB = 2 : 3$. Given $\vec{OA} = 3\vec{x} + 2\vec{y}$, $\vec{OC} = 9\vec{x} + 2\vec{y}$ and $\vec{CB} = 3r\vec{y}$, where r is constant,

(a) ungkapkan dalam sebutan $\vec{x}$ dan/atau $\vec{y}$,

express in terms of $\vec{x}$ and/or $\vec{y}$.

(i) $\vec{AC}$

(ii) $\vec{OM}$

[3 markah/marks]

(b) ungkapkan $\vec{OB}$ dalam sebutan
express $\vec{OB}$ in terms of

(i) $\vec{x}$ dan $\vec{y}$

(ii) $\vec{x}$, $\vec{y}$ dan r .

Seterusnya, cari nilai r .

Hence, find the value of r .

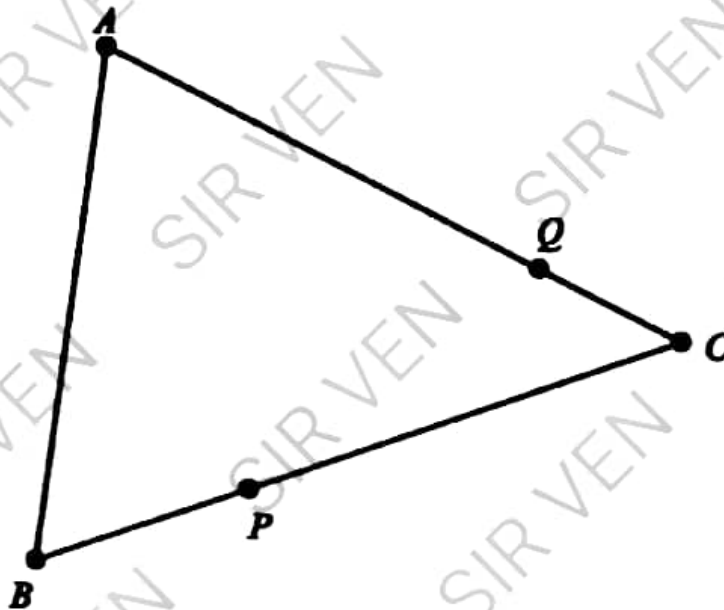
[5 markah /marks]

(a)(i)	$\overrightarrow{AC} = \overrightarrow{AO} + \overrightarrow{OC}$ $= -3\underline{x} - 2\underline{y} + 9\underline{x} + 2\underline{y}$ $= 6\underline{x}$	N1
(a)(ii)	$\overrightarrow{OM} = \overrightarrow{OA} + \overrightarrow{AM}$ $= \overrightarrow{OA} + \frac{1}{2}\overrightarrow{AC}$ $= 3\underline{x} + 2\underline{y} + \frac{1}{2}(6\underline{x})$ $= 6\underline{x} + 2\underline{y}$	K1 N1
(b)(i)	$\overrightarrow{OB} = \frac{3}{2}\overrightarrow{OM}$ $= \frac{3}{2}(6\underline{x} + 2\underline{y})$ $= 9\underline{x} + 3\underline{y}$	K1 N1
(b)(ii)	$\overrightarrow{OB} = \overrightarrow{OC} + \overrightarrow{CB}$ $= 9\underline{x} + 2\underline{y} + 3r\underline{y}$ $= 9\underline{x} + (2 + 3r)\underline{y}$ With compare, $2 + 3r = 3$ $r = \frac{1}{3}$	K1 K1 N1

Q10: PERAK

Rajah 1 menunjukkan sebuah segi tiga ABC . Titik P and Q terletak pada BC dan AC masing-masing.

Diagram 1 shows a triangle ABC . Points P and Q lie on BC and AC respectively.



Rajah 1
Diagram 1

Diberi $\vec{BP} = 4\vec{x}$, $\vec{BA} = 20\vec{y}$, $BP : PC = 1 : 2$ dan $AQ : AC = 3 : n$, dengan keadaan n ialah suatu pemalar.

It is given $\vec{BP} = 4\vec{x}$, $\vec{BA} = 20\vec{y}$, $BP : PC = 1 : 2$ and $AQ : AC = 3 : n$, where n is a constant.

(a) Cari nilai n jika $\vec{CQ} = -3\vec{x} + 5\vec{y}$. [3 markah]

Find the value of n if $\vec{CQ} = -3\vec{x} + 5\vec{y}$. [3 marks]

(b) Diberi $\vec{x} = 3\vec{i}$ dan $\vec{y} = \vec{i} - \frac{3}{5}\vec{j}$, cari vektor unit dalam arah $\vec{CA}$. [3 markah]

Given $\vec{x} = 3\vec{i}$ and $\vec{y} = \vec{i} - \frac{3}{5}\vec{j}$, find the unit vector in the direction $\vec{CA}$. [3 marks]

$$1(a) \quad \overrightarrow{CB} + \overrightarrow{BA} \text{ atau } \overrightarrow{AB} + \overrightarrow{BC}$$

$$\frac{n-3}{n}(-12\tilde{x} + 20\tilde{y}) = -3\tilde{x} + 5\tilde{y} \text{ dan perbandingan salah}$$

komponen dilakukan

4 (atau $n = 4$)

$$(b) \quad -12(3\tilde{i}) + 20\left(\tilde{i} - \frac{3}{5}\tilde{j}\right)$$

$$\frac{-16\tilde{i} - 12\tilde{j}}{\sqrt{(-16)^2 + (-12)^2}}$$

$$-\frac{4}{5}\tilde{i} - \frac{3}{5}\tilde{j}$$

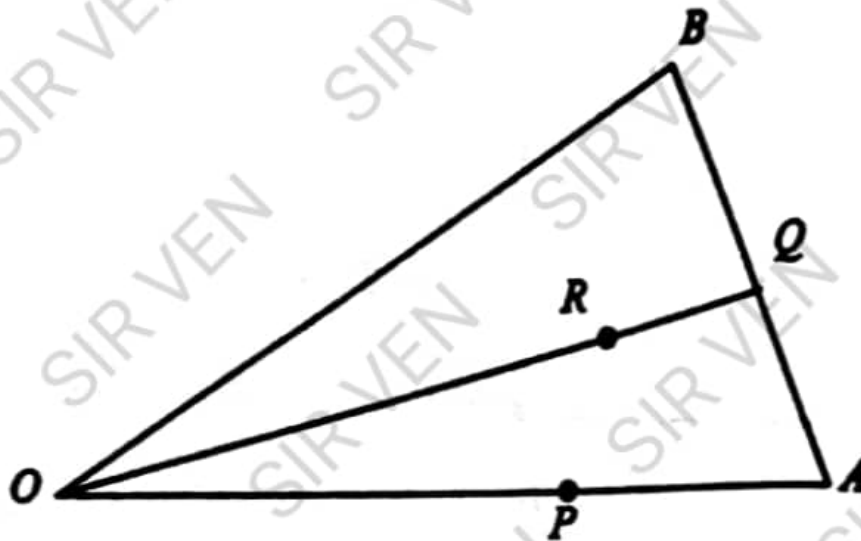
Q11: NEGERI SEMBILAN

Dalam Rajah 5, OAB ialah satu segitiga, $OP = \frac{2}{3}OA$, $AB = 2AQ$, dan $OR = \frac{4}{5}OQ$.

Diberi bahawa $\overrightarrow{OA} = 9\underline{x}$ dan $\overrightarrow{OB} = 4\underline{y}$.

In Diagram 5, OAB is a triangle, $OP = \frac{2}{3}OA$, $AB = 2AQ$, and $OR = \frac{4}{5}OQ$.

Given that $\overrightarrow{OA} = 9\underline{x}$ and $\overrightarrow{OB} = 4\underline{y}$.



Rajah 5
Diagram 5

(a) Ungkapkan, dalam sebutan $\underline{x}$ dan/atau $\underline{y}$,

[3 markah]

Express, in terms of $\underline{x}$ and/or $\underline{y}$,

[3 marks]

(i) $\overrightarrow{PB}$,

(ii) $\overrightarrow{OQ}$.

(b) Seterusnya, buktikan bahawa titik-titik P , R dan B adalah segaris.

[4 markah]

Hence, prove that points P , R and B are collinear.

[4 marks]

(c) Diberi luas ΔPAB ialah 12 cm^2 . Cari luas ΔOAB .

[2 markah]

Given the area of ΔPAB is 12 cm^2 . Find the area of ΔOAB .

[2 marks]

(a) $\overrightarrow{PB} = \overrightarrow{PO} + \overrightarrow{OB}$ atau $\overrightarrow{PB} = \overrightarrow{PA} + \overrightarrow{AB}$ atau $\overrightarrow{OQ} = \overrightarrow{OA} + \overrightarrow{AQ}$ atau setara

(i) $\overrightarrow{PB} = -6\underline{x} + 4\underline{y}$

(ii) $\overrightarrow{OQ} = \frac{9}{2}\underline{x} + 2\underline{y}$

(b) $\overrightarrow{PR} = -\frac{12}{5}\underline{x} + \frac{8}{5}\underline{y}$ atau setara

Bandingkan pekali $\underline{x}$ atau $\underline{y}$:

$-\frac{12}{5} = -6\lambda$ atau $\frac{8}{5} = 4\lambda$ atau setara

$\lambda = \frac{2}{5}$ atau setara

$\overrightarrow{PR} = \frac{2}{5}\overrightarrow{PB}$ atau setara

(c) $\frac{1}{2} 3\underline{x} h = 12$	ATAU	$\frac{1}{2}(3PA)h$	ATAU	$\frac{OAB}{PAB} = \frac{3}{1}$
$\frac{1}{2} 9\underline{x} \left(\frac{8}{ \underline{x} }\right)$		3×12		$OAB = 3(12)$
36		36		36

Q12: KELANTAN

Titik A dan titik B mempunyai vektor kedudukan $\underline{a}$ dan $\underline{b}$ masing-masing relatif kepada titik O . Diberi L ialah titik tengah $\overline{OA}$ dan M ialah titik pada garis $\overline{OB}$ yang dipanjangkan dengan keadaan $\overline{OM} = 3\overline{OB}$. P ialah titik pada $\overline{LM}$ dengan keadaan $\overline{LP} = k\overline{LM}$.

Points A and B have position vectors $\underline{a}$ and $\underline{b}$ respectively relative to point O . Given that L is a midpoint of $\overline{OA}$ and M is the point on $\overline{OB}$ produced such that $\overline{OM} = 3\overline{OB}$. P is the point on $\overline{LM}$ such that $\overline{LP} = k\overline{LM}$.

(a) Ungkapkan $\overline{LM}$ dalam sebutan $\underline{a}$ dan $\underline{b}$

[2 markah]

Express $\overline{LM}$ in terms of $\underline{a}$ and $\underline{b}$

[2 marks]

(b) Ungkapkan $\overline{AP}$ dalam sebutan $\underline{a}$, $\underline{b}$ dan k

[2 markah]

Express $\overline{AP}$ in terms of $\underline{a}$, $\underline{b}$ and k

[2 marks]

(c) Jika A , P dan B ialah segaris, cari

If A , P and B are collinear, find

i). k

ii). $\frac{\overline{AP}}{\overline{PB}}$

[6 markah]

[6 marks]

9 (a)

$$LM = LO + OM$$

$$LM = -\frac{1}{2}a + 3b$$

9 (b)

$$AP = -\frac{1}{2}a + kLM$$

$$AP = \left(-\frac{1}{2} - \frac{1}{2}k\right)a + 3kb$$

9(c)(i)

$$\left(-\frac{1}{2} - \frac{1}{2}k\right)a + 3kb = \lambda(-a + b)$$

$$\left(-\frac{1}{2} - \frac{1}{2}k\right) = -\lambda \text{ dan } 3k = \lambda$$

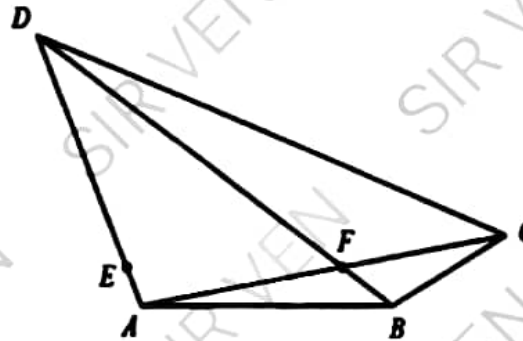
$$\left(-\frac{1}{2} - \frac{1}{2}k\right) = -3k, (\text{hapuskan satu unknown})$$

$$k = \frac{1}{5}$$

Q13: JOHOR

Rajah 9 menunjukkan sisi empat $ABCD$. Pepenjuru-pepenjuru BD dan AC bersilang di titik F . Titik E terletak pada AD .

Diagram 9 shows a quadrilateral $ABCD$. The diagonals BD and AC intersect at point F . Point E lies on AD .



Rajah 9/Diagram 9

Diberi bahawa $\vec{AE} = \frac{1}{5} \vec{AD}$, $\vec{BF} = \frac{1}{5} \vec{BD}$, $\vec{AB} = \underline{x}$ and $\vec{AE} = \underline{y}$.

It is given that $\vec{AE} = \frac{1}{5} \vec{AD}$, $\vec{BF} = \frac{1}{5} \vec{BD}$, $\vec{AB} = \underline{x}$ and $\vec{AE} = \underline{y}$.

(a) Ungkapkan dalam sebutan $\underline{x}$ dan $\underline{y}$

Express in terms of $\underline{x}$ and $\underline{y}$

(i) $\vec{DB}$

(ii) $\vec{AF}$

[5 markah/ marks]

(b) Diberi $\vec{DC} = m\underline{x} - \underline{y}$ dan $\vec{AF} = n\vec{AC}$, dengan keadaan m dan n ialah pemalar, cari nilai m dan n .

Given that $\vec{DC} = m\underline{x} - \underline{y}$ and $\vec{AF} = n\vec{AC}$, where m and n are constants, find the value of m and n .

[5 markah/ marks]

Jawapan / Answer:

$$(a) (i) \overrightarrow{DB} = \overrightarrow{DA} + \overrightarrow{AB}$$

$$= -5\overrightarrow{AE} + x$$

$$= x - 5y$$

$$(ii) \overrightarrow{AF} = \overrightarrow{AB} + \overrightarrow{BF}$$

$$= c + \frac{1}{5}(-x + 5y)$$

$$= \frac{4}{5}x + y$$

$$(b) \quad \overrightarrow{DC} = mx - y$$

$$\overrightarrow{AC} = \overrightarrow{AD} + \overrightarrow{DC}$$

$$\overrightarrow{AC} = 5y + mx - y$$

$$= mx + 4y$$

$$\overrightarrow{AF} = n \overrightarrow{AC}$$

$$\frac{4}{5}x + y = n(mx + 4y)$$

$$\frac{4}{5}x + y = mnx + 4ny$$

Bandingkan x dan y

$$1 = 4n$$

$$n = \frac{1}{4}$$

$$\frac{4}{5} = mn$$

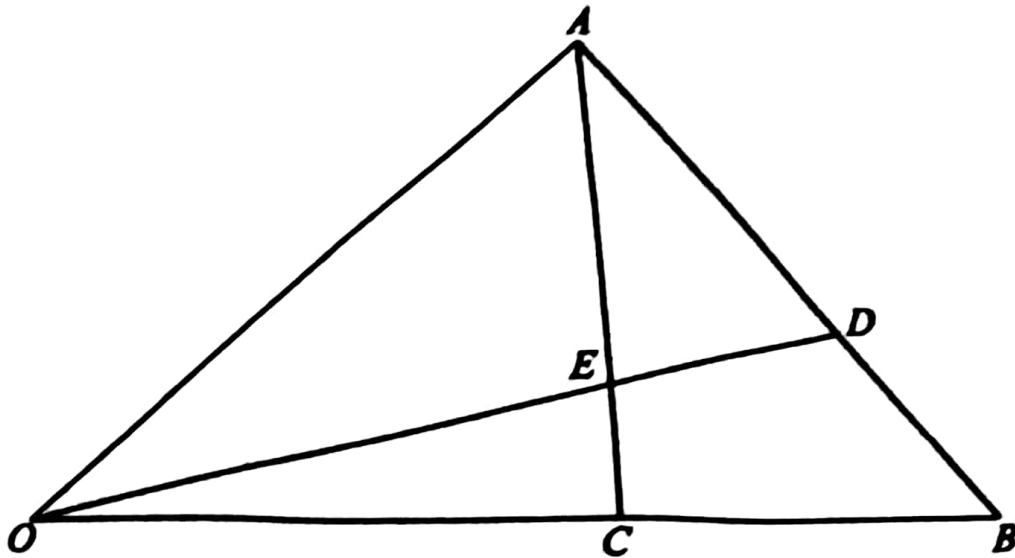
$$\frac{4}{5} = m\left(\frac{1}{4}\right)$$

$$m = \frac{16}{5}$$

Q14: SBP (ASRAMA)

Rajah 2 menunjukkan sebuah segi tiga OAB . Titik C dan titik D masing-masing terletak pada garis lurus OB dan garis lurus AB . Garis lurus OD dan garis lurus AC bersilang pada titik E .

Diagram 2 shows a triangle OAB . Point C and point D are on the straight lines OB and AB respectively. Straight lines OD and AC intersect at point E .



Rajah 2
Diagram 2

Diberi bahawa $\overline{OA} = x$, $\overline{OB} = y$, $3\overline{AD} = 2\overline{AB}$ dan $\overline{OC} = \frac{3}{5}\overline{OB}$.

Given that $\overline{OA} = x$, $\overline{OB} = y$, $3\overline{AD} = 2\overline{AB}$ and $\overline{OC} = \frac{3}{5}\overline{OB}$.

(a) Ungkapkan dalam sebutan x dan y :

Express in terms of x and y :

(i) $\overline{AC}$,

(ii) $\overline{OD}$.

[3 markah]

[3 marks]

(b) Diberi bahawa $\overrightarrow{OE} = h\overrightarrow{OD}$ dan $\overrightarrow{AE} = k\overrightarrow{AC}$, dengan keadaan h dan k ialah pemalar.

It is given that $\overrightarrow{OE} = h\overrightarrow{OD}$ and $\overrightarrow{AE} = k\overrightarrow{AC}$, where h and k are constants.

Ungkapkan $\overrightarrow{OE}$ dalam sebutan

Express $\overrightarrow{OE}$ in terms of

(i) h , $\underline{x}$ dan / and $\underline{y}$,

(ii) k , $\underline{x}$ dan / and $\underline{y}$.

[3 markah]

[3 marks]

(c) Seterusnya, cari nilai-nilai h dan k .

Hence, find the values of h and k .

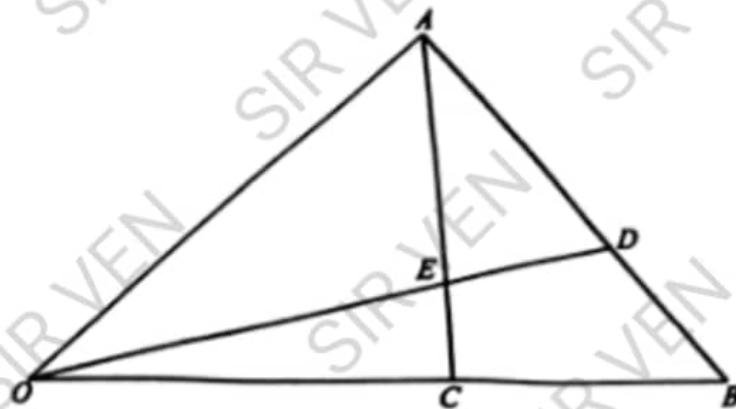
[4 markah]

[4 marks]

Q14: SBP (ASRAMA)

Rajah 2 menunjukkan sebuah segi tiga OAB . Titik C dan titik D masing-masing terletak pada garis lurus OB dan garis lurus AB . Garis lurus OD dan garis lurus AC bersilang pada titik E .

Diagram 2 shows a triangle OAB . Point C and point D are on the straight lines OB and AB respectively. Straight lines OD and AC intersect at point E .



Rajah 2
Diagram 2

Diberi bahawa $\overrightarrow{OA} = \underline{x}$, $\overrightarrow{OB} = \underline{y}$, $3\overrightarrow{AD} = 2\overrightarrow{AB}$ dan $\overrightarrow{OC} = \frac{3}{5}\overrightarrow{OB}$.

Given that $\overrightarrow{OA} = \underline{x}$, $\overrightarrow{OB} = \underline{y}$, $3\overrightarrow{AD} = 2\overrightarrow{AB}$ and $\overrightarrow{OC} = \frac{3}{5}\overrightarrow{OB}$.

(a) Ungkapkan dalam sebutan $\underline{x}$ dan $\underline{y}$:

Express in terms of $\underline{x}$ and $\underline{y}$:

- (i) $\overrightarrow{AC}$,
- (ii) $\overrightarrow{OD}$.

[3 markah]

[3 marks]

(b) Diberi bahawa $\overrightarrow{OE} = h\overrightarrow{OD}$ dan $\overrightarrow{AE} = k\overrightarrow{AC}$, dengan keadaan h dan k ialah pemalar.

It is given that $\overrightarrow{OE} = h\overrightarrow{OD}$ and $\overrightarrow{AE} = k\overrightarrow{AC}$, where h and k are constants.

Ungkapkan $\overrightarrow{OE}$ dalam sebutan

Express $\overrightarrow{OE}$ in terms of

(i) h , $\underline{x}$ dan / and $\underline{y}$,

(ii) k , $\underline{x}$ dan / and $\underline{y}$.

[3 markah]

[3 marks]

(c) Seterusnya, cari nilai-nilai h dan k .

Hence, find the values of h and k .

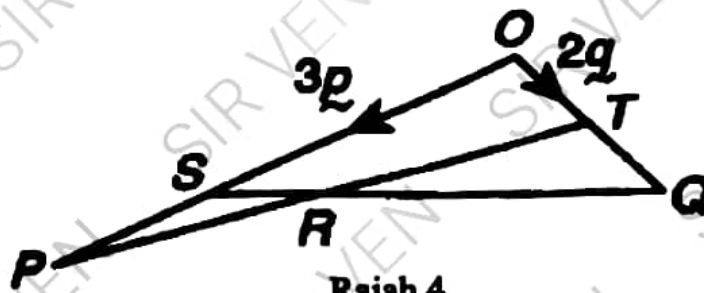
[4 markah]

[4 marks]

Q15: KELATAN MIMS (SET 1)

Rajah 4 menunjukkan segitiga OPT dan OQS .

Diagram 4 shows the triangle of OPT and OQS .



Rajah 4

Diagram 4

- (a) Diberi $\overrightarrow{OP} = 3\mathbf{p}$ dan $\overrightarrow{OQ} = 2\mathbf{q}$. T ialah titik tengah bagi OQ dan S terletak di atas OP dengan keadaan $\overrightarrow{OS} = \frac{2}{3}\overrightarrow{OP}$. Ungkapkan dalam sebutan $\mathbf{p}$ dan $\mathbf{q}$,

Given that $\overrightarrow{OP} = 3\mathbf{p}$ dan $\overrightarrow{OQ} = 2\mathbf{q}$. T is the midpoint of OQ and S lies on OP where

$\overrightarrow{OS} = \frac{2}{3}\overrightarrow{OP}$. Express in terms of $\mathbf{p}$ and $\mathbf{q}$,

- $\overrightarrow{QS}$,
- $\overrightarrow{TP}$.

[3 markah]

[3 marks]

- (b) Diberi $\overrightarrow{RS} = h\overrightarrow{QS}$ dan $\overrightarrow{RP} = k\overrightarrow{TP}$ dengan keadaan h dan k ialah pemalar, ungkapkan

Given $\overrightarrow{RS} = h\overrightarrow{QS}$ and $\overrightarrow{RP} = k\overrightarrow{TP}$ where h and k are constants, express

- $\overrightarrow{RS}$ dalam sebutan h , $\mathbf{p}$ dan / atau $\mathbf{q}$,

$\overrightarrow{RS}$ in terms of h , $\mathbf{p}$ and / or $\mathbf{q}$,

- $\overrightarrow{RP}$ dalam sebutan k , $\mathbf{p}$ and / atau $\mathbf{q}$.

$\overrightarrow{RP}$ in terms of k , $\mathbf{p}$ and / or $\mathbf{q}$.

Seterusnya cari nilai h dan nilai k .

Hence, find the value of h and of k .

[5 markah]

[5 marks]

5 (a)

(i)(ii)

$$\overrightarrow{QS} = \overrightarrow{QO} + \overrightarrow{OS} \quad \text{or} \quad \overrightarrow{TP} = \overrightarrow{TO} + \overrightarrow{OP}$$

$$2\vec{p} - 2\vec{q}$$

$$3\vec{p} - \vec{q}$$

(b)(i)(ii)

$$2h\vec{p} - 2h\vec{q}$$

$$3k\vec{p} - k\vec{q}$$

$$\vec{p} = -2h\vec{p} + 2h\vec{q} + 3k\vec{p} - k\vec{q}$$

$$h = \frac{1}{4}$$

$$k = \frac{1}{2}$$

Q16: TERENGGANU

Diberi bahawa OAB ialah sebuah segi tiga. Titik C terletak pada OA dan titik D terletak pada AB . Garis lurus BC bersilang dengan garis lurus OD pada titik E .

Diberi $OA:OC = 4:3$, $AB:AD = 2:1$, $\overrightarrow{OA} = 20\mathbf{x}$ dan $\overrightarrow{OB} = 9\mathbf{y}$.

Given that OAB is a triangle. Point C lies on OA and point D lies on AB .

The straight line BC intersects the straight line OD at point E .

It is given that $OA:OC = 4:3$, $AB:AD = 2:1$, $\overrightarrow{OA} = 20\mathbf{x}$ and $\overrightarrow{OB} = 9\mathbf{y}$.

(a) Ungkapkan dalam sebutan $\mathbf{x}$ dan/atau $\mathbf{y}$,

Express in terms of $\mathbf{x}$ and/or $\mathbf{y}$,

(i) $\overrightarrow{BC}$

(ii) $\overrightarrow{OD}$

[3 markah]

[3 marks]

(b) Jika $\overrightarrow{BE} = m\overrightarrow{BC}$ dan $\overrightarrow{OE} = n\overrightarrow{OD}$, dengan keadaan m dan n adalah pemalar,

Cari nilai m dan n .

[5 markah]

If $\overrightarrow{BE} = m\overrightarrow{BC}$ and $\overrightarrow{OE} = n\overrightarrow{OD}$, such that m and n are constants, find the values of m and of n .

[5 marks]

(c) Diberi bahawa $|x| = 2$ unit dan luas segi tiga OAB ialah 140 unit^2 .

Hitung jarak serenjang dari B ke OA .

[2 markah]

It is given that $|x| = 2$ unit and the area of the triangle OAB is 140 unit^2 .

Calculate the perpendicular distance from B to OA .

[2 marks]

(a) $\overrightarrow{BC} = \overrightarrow{BO} + \overrightarrow{OC}$ atau $\overrightarrow{OD} = \overrightarrow{OA} + \overrightarrow{AD}$ dan

$$\overrightarrow{BC} = -9\underline{x} + \frac{3}{4}(20\underline{x}) \text{ atau } \overrightarrow{OD} = 20\underline{x} + \frac{1}{2}(-20\underline{x} + 9\underline{y})$$

K1

(i) $15\underline{x} - 9\underline{y}$

N1

(ii) $10\underline{x} + \frac{9}{2}\underline{y}$

N1

(b) $\overrightarrow{BE} = -9\underline{y} + n\left(10\underline{x} + \frac{9}{2}\underline{y}\right)$

K1

$$m(15\underline{x} - 9\underline{y}) = -9\underline{y} + n\left(10\underline{x} + \frac{9}{2}\underline{y}\right)$$

K1

$$15m = 10n, \quad -9m = \frac{9}{2}n - 9 \text{ dan selesaikan}$$

K1

$$m = \frac{4}{7}, n = \frac{6}{7}$$

N1 N1

(c) $\frac{1}{2}(20 \times 2)h = 140$

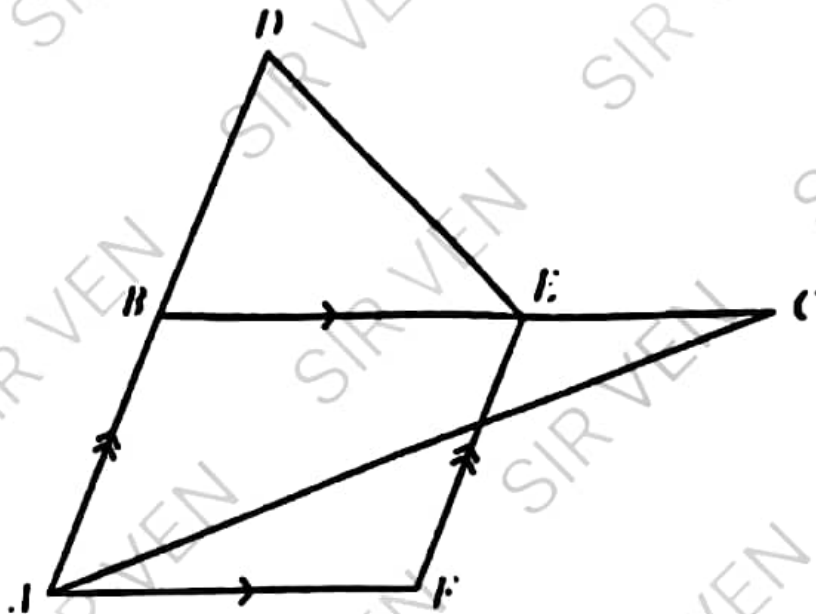
K1

$$h = 7$$

N1

Q17: MRSM

- (a) Rajah 5 menunjukkan trapezium $ADEF$ dan segitiga ABC .
Diagram 5 shows trapezium $ADEF$ and triangle ABC .



Rajah 5
Diagram 5

Diberi bahawa $\overline{AD} = 8x$, $\overline{BE} = 3y$, $\overline{BE} = \frac{3}{5}\overline{BC}$ dan nisbah $AD:FE = 2:1$.

It is given that $\overline{AD} = 8x$, $\overline{BE} = 3y$, $\overline{BE} = \frac{3}{5}\overline{BC}$ and ratio $AD:FE = 2:1$.

- (i) Ungkapkan $\overline{AC}$ dalam sebutan x dan/atau y .
Express $\overline{AC}$ in terms of x and/or y .

[3 markah]

[3 marks]

- (ii) Garis FE dipanjangkan kepada titik M dengan keadaan $\overline{FM} = \frac{8}{5}\overline{FE}$ dan $\overline{BM} = k\overline{AC}$.
Cari nilai k .

[4 markah]

Line FE is extended to a point M such that $\overline{FM} = \frac{8}{5}\overline{FE}$ and $\overline{BM} = k\overline{AC}$.

Find the value of k .

[4 marks]